

C12 - 6.0 - Fractions/LCD/Exponents/Distribution Theory

Multiply

$$\frac{a}{b} \times \frac{c}{d} = \frac{ac}{bd}$$

$$a \times \frac{b}{c} = \frac{ab}{c}$$

$$\frac{a}{b} \times c = \frac{ac}{b}$$

$$\frac{1}{a} \times a = 1$$

Divide

$$\begin{aligned}\frac{a}{b} \div \frac{c}{d} &= \frac{\left(\frac{a}{b}\right)}{\left(\frac{c}{d}\right)} \\ \frac{a}{b} \times \frac{d}{c} &= ad \\ \frac{a}{b} \times \frac{c}{c} &= bc\end{aligned}$$

$$\begin{aligned}\frac{a}{b} \div \frac{b}{c} &= \frac{\left(\frac{a}{b}\right)}{\left(\frac{b}{c}\right)} \\ a \times \frac{c}{b} &= ac \\ a \times \frac{c}{c} &= cb\end{aligned}$$

$$\begin{aligned}\frac{a}{b} \div c &= \frac{\left(\frac{a}{b}\right)}{\left(\frac{c}{c}\right)} \\ \frac{a}{b} \times \frac{1}{c} &= \frac{a}{bc} \\ \frac{a}{b} \times \frac{c}{c} &= \frac{a}{bc}\end{aligned}$$

Add/Subtract

$$\frac{a}{b} + \frac{c}{b} = \frac{a+c}{b} \quad \frac{a}{b} + \frac{c}{d} = \frac{ad+cb}{bd} \quad \frac{a}{b} + \frac{c}{bd} = \frac{ad+cb}{bd} \quad \frac{a}{b^2} + \frac{c}{b} = \frac{a+cb}{b^2} \quad \frac{a}{b} + \frac{c}{b+1} = \frac{a(b+1)+cb}{b(b+1)}$$

$$\frac{a+b}{c} = \frac{a}{c} + \frac{b}{c} \quad \text{Separate} \quad \frac{a}{b+c} \neq \frac{a}{b} + \frac{a}{c} \quad \text{Common Mistakes} \quad \cancel{\frac{x+a}{x}} \neq 1+a \quad \frac{x+a}{x} = \frac{x}{x} + \frac{a}{x}$$

$$a+b+c = a+c+b$$

Rearrange

$$ab = ba$$

Mirror

$$\text{Reciprocal: } \frac{a}{b} \rightarrow \frac{b}{a}$$

$$\frac{a}{b} = \frac{c}{d}$$

Cross Multiply

$$\frac{a}{b} = \frac{c}{d}$$

$$a = \frac{cb}{d}$$

$$\frac{da}{b} = c$$

$$\frac{da}{c} = b$$

$$d = \frac{cb}{a}$$

$$\begin{aligned}\frac{x}{2} &= \frac{1}{2} \\ x &= 1 \\ \frac{x}{2} &= \frac{1}{2} \\ x &= 1\end{aligned}$$

$$\frac{x}{4} = \frac{1}{4} + \frac{2}{4}$$

Multiply Both Sides By LCD

$$\begin{aligned}\frac{1}{x} + 1 &= \frac{1+x}{2x+3} \\ 2 + \frac{3}{x} &= \frac{2x+3}{2x+3}\end{aligned}$$

Multiply Top/Bottom By LCD

$$x \times x = x^2$$

$$x \times x^2 = x^3$$

$$x^m \times x^n = x^{m+n}$$

$$\frac{x^2}{x}$$

$$\frac{x^3}{x^2}$$

$$\frac{x^3}{x}$$

$$\frac{x}{x}$$

$$\frac{x^m}{x^n} = x^{m-n}$$

$$(x^m)^n = x^{m \times n}$$

$$x^{-a} = \frac{1}{x^a}$$

$$\frac{1}{x^a} = x^{-a}$$

$$\frac{2^{-3}-1}{x} = \frac{\frac{1}{2^3}-1}{x} \neq \frac{-1}{2^{-3}x}$$

$$\text{Common Mistakes}$$

$$x^{\frac{m}{n}} = \sqrt[n]{x^m}$$

$$\begin{aligned}x(x+1) \\ x^2 + x\end{aligned}$$

$$\begin{aligned}(x-2)(x+1) \\ x^2 - x - 2\end{aligned}$$

$$\begin{aligned}(2x+1)(x+1) \\ 2x^2 + 3x + 1\end{aligned}$$

$$\begin{aligned}(x+1)(x-1) \\ x^2 - 1\end{aligned}$$

FOIL Conjugates: FL

$$\begin{aligned}x^2 + x \\ x(x+1)\end{aligned}$$

$$\begin{aligned}x^2 - x - 2 \\ (x-2)(x+1)\end{aligned}$$

$$\begin{aligned}2x^2 + 3x + 1 \\ (2x+1)(x+1)\end{aligned}$$

$$\begin{aligned}x^2 - 1 \\ (x+1)(x-1)\end{aligned}$$