

# C12 - 6.0 - Fractions/LCD/Exponents/Distribution Theory

Multiply	$\frac{a}{b} \times \frac{c}{d} = \frac{ac}{bd}$	$a \times \frac{b}{c} = \frac{ab}{c}$	$\frac{a}{b} \times c = \frac{ac}{b}$	$\frac{1}{a} \times a = 1$
Divide	$\frac{\left(\frac{a}{b}\right)}{\left(\frac{c}{d}\right)} = \frac{a}{b} \times \frac{d}{c} = \frac{ad}{bc}$	$a \div \frac{b}{c} = a \times \frac{c}{b} = \frac{ac}{b}$	$\frac{a}{b} \div c = \frac{a}{b} \times \frac{1}{c} = \frac{a}{bc}$	$\frac{\left(\frac{a}{b}\right)}{c} = \frac{a}{b} \div c = \frac{a}{bc}$

Add/Subtract

$\frac{a}{b} + \frac{c}{b} = \frac{a+c}{b}$	$\frac{a}{b} + \frac{c}{d} = \frac{ad+cb}{bd}$	$\frac{a}{b} + \frac{c}{bd} = \frac{ad+c}{bd}$	$\frac{a}{b^2} + \frac{c}{b} = \frac{a+cb}{b^2}$	$\frac{a}{b} + \frac{c}{b+1} = \frac{a(b+1)+cb}{b(b+1)}$
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Common Mistakes

$\frac{a+b}{c} = \frac{a}{c} + \frac{b}{c}$ Separate	$\frac{a}{b+c} \neq \frac{a}{b} + \frac{a}{c}$	$\frac{x+a}{x} \neq 1+a$	$\frac{x+a}{x} = \frac{x}{x} + \frac{a}{x}$
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$a+b+c = a+c+b$ Rearrange	$ab = ba$ Mirror	Reciprocal: $\frac{a}{b} \rightarrow \frac{b}{a}$
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$\frac{a}{b} = \frac{c}{d}$ $da = cb$	Cross Multiply	$\frac{a}{b} = \frac{c}{d}$	$a = \frac{cb}{d}$	$\frac{da}{b} = c$	$\frac{da}{c} = b$	$d = \frac{cb}{a}$
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$\frac{x}{2} = \frac{1}{2}$ $\frac{x}{x} = \frac{1}{1}$ $\frac{x}{2} = \frac{1}{2}$ $x = 1$	$\frac{x}{4} = \frac{1}{4} + \frac{2}{4}$	Multiply Both Sides By LCD	$\frac{1}{x} + 1 = \frac{1+x}{2x+3}$ Multiply Top/Bottom By LCD
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$x \times x = x^2$	$x \times x^2 = x^3$	$x^m \times x^n = x^{m+n}$	$\frac{x^2}{x} = x$	$\frac{x^3}{x^2} = x$	$\frac{x^3}{x} = x^2$	$\frac{x}{x} = 1$	$\frac{x^m}{x^n} = x^{m-n}$
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$(x^m)^n = x^{m \times n}$	$x^{-a} = \frac{1}{x^a}$	$\frac{1}{x^a} = x^{-a}$	$\frac{2^{-3} - 1}{x} = \frac{1}{2^3} - 1 \neq \frac{-1}{2^{-3}x}$ Common Mistakes	$\frac{m}{x^n} = \sqrt[n]{x^m}$
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$x(x+1)$ $x^2 + x$	$(x-2)(x+1)$ $x^2 - x - 2$	$(2x+1)(x+1)$ $2x^2 + 3x + 1$	$(x+1)(x-1)$ $x^2 - 1$	FOIL Conjugates: FL
$x^2 + x$ $x(x+1)$	$x^2 - x - 2$ $(x-2)(x+1)$	$2x^2 + 3x + 1$ $(2x+1)(x+1)$	$x^2 - 1$ $(x+1)(x-1)$	