

C12 - 8.3 - $\log a^m = m \log a$ Change Base Dist. Notes

$$\begin{array}{c} \log 5^2 \\ \updownarrow \\ 2 \log 5 \\ \updownarrow \\ \log \sqrt{x} \\ \log x^{\frac{1}{2}} \\ \updownarrow \\ \frac{1}{2} \log x \\ \updownarrow \\ \frac{\log x}{2} \end{array}$$

$$\begin{array}{c} \log x^2 \\ \updownarrow \\ 2 \log x \\ \updownarrow \\ \log \left(\frac{1}{2} \right) \\ \log 2^{-1} \\ -1 \log 2 \\ \updownarrow \\ -\log 2 \end{array}$$

| | | |
|---------------------|----|-----------------------|
| $3 \log 4^2$ | OR | $3 \log 4^2$ |
| $2 \times 3 \log 4$ | | $\log 4^{2 \times 3}$ |
| $6 \log 4$ | | $\log 4^6$ |
| | | $6 \log 4$ |

Bring Exponent down in front and Vice Versa Multiply

| | | | | |
|--|--------------------------|---|---|---|
| $\log_5 5^4 = x$ $5^4 = 5^x$ $x = 4$ | 5 to what power is 5^4 | $\log_5 625 = x$ $\log_5 5^4 = x$ $4 \log_5 5 = x$ $4 \times 1 = x$ $x = 4$ | Change of Base Bring Exponent down in front Log Rules $\log_5 5 = 1$ | $\log_5 625 = x$ $625 = 5^x$ $5^4 = 5^x$ $x = 4$ |
|--|--------------------------|---|---|---|

$$\begin{array}{l} \log xy^2 = \\ \log x + \log y^2 = \\ \log x + 2 \log y \end{array}$$

The exponent only applies to the y value

| | | |
|-------------------------|--------------|------------------------|
| $\log x^2 y^2 =$ | \leftarrow | $\log (xy)^2 =$ |
| $\log x^2 + \log y^2 =$ | | $2 \log xy =$ |
| $2 \log x + 2 \log y$ | | $2(\log x + \log y) =$ |
| | | $2 \log x + 2 \log y$ |

$$\log 3^{x+2}$$

Bring Exponent in front

$$(x+2) \log 3$$

Distribute

$$3x \log 7 - x \log 2 =$$

$$x(3 \log 7 - \log 2)$$

GCF = x

Change of Base

$$\frac{\log 16}{\log 4} =$$

$$\log_4 16 = 2$$

$$\frac{\log_2 16}{\log_2 4} =$$

$$\log_4 16 = 2$$

Exponential Form

$$16 = 4^2$$

$$\log_2 2 = 2$$

$$\log_2 16 = 4$$

$$\frac{4}{2} = 2$$

$\log_2 4 =$ Choose the Base you want!

$$\frac{\log_5 4}{\log_5 2}$$

$$\log_8 16 =$$

$$\frac{\log_2 16}{\log_2 8} = \frac{4}{3}$$

$$\frac{1}{\log_8 2} =$$

$$\frac{1}{\frac{\log 2}{\log 8}} =$$

$$1 \times \frac{\log 8}{\log 2} = \frac{\log 8}{\log 2}$$

Rule 6

$$\log_3 9 + \log_9 2$$

$$\log_{(3)^2} (9)^2 + \log_9 2$$

$$\log_9 81 + \log_9 2$$

$$\log_9 81 \times 2$$

Take the base and the log to any exponent you like!

$$\log_9 162$$