

P11 - 1.3 - Isolating variables Notes Algebra

$a + b = c$

Solve for "a"

$\begin{matrix} \curvearrowright \\ + = - \\ \curvearrowleft \end{matrix}$

$a + b = c$
 $-b -b$
 $a = c - b$

Subtract "b" from both sides
Mirror

$a + b = c$
 $a = c - b$

Bring "b" over, change sign

$v = \frac{d}{t}$

Solve for d

$v = \frac{d}{t}$
 $t \times v = \frac{d}{t} \times t$
 $tv = d$
 $d = vt$

\times both sides by "t"
Simplify
Mirror

$v = \frac{d}{t}$

Solve for t

$v = \frac{d}{t}$
 $t \times v = \frac{d}{t} \times t$
 $tv = d$
 $\frac{t}{b} = \frac{d}{v}$
 $t = \frac{d}{v}$

\times both sides by "t"
 \div both sides by "v"
 Bring t up
 Bring v down

$v = \frac{d}{t}$
 $tv = d$
 $d = vt$

Bring t up
Mirror

Just cross multiply!

$v = \frac{d}{t}$
 $t = \frac{d}{v}$

Switch v and t

$\frac{a}{b} = \frac{c}{d}$

Solve for "a"

$\frac{a}{b} = \frac{c}{d}$
 $a = \frac{cb}{d}$

Bring "b" up

Solve for c

$\frac{a}{b} = \frac{c}{d}$
 $\frac{ad}{b} = c$
 $c = \frac{ad}{b}$

Bring "d" up
Mirror

Solve for b

$\frac{a}{b} = \frac{c}{d}$
 $a = \frac{cb}{d}$
 $ad = cb$
 $\frac{ad}{c} = b$
 $b = \frac{ad}{c}$

Bring b up
 Bring d up
 Bring c down
 Mirror

Solve for "d"

$\frac{a}{b} = \frac{c}{d}$
 $\frac{ad}{b} = c$
 $ad = cb$
 $d = \frac{cb}{a}$

Bring d up
 Bring b up
 Bring "a" down

$\sin\theta = \frac{O}{H}$
 $O = H\sin\theta$

$\sin\theta = \frac{O}{H}$
 $H = \frac{\sin\theta}{O}$

$\cos\theta = \frac{A}{H}$
 $A = H\cos\theta$

$\cos\theta = \frac{A}{H}$
 $H = \frac{A}{\cos\theta}$

$\tan\theta = \frac{O}{A}$
 $O = A\tan\theta$

$\tan\theta = \frac{O}{A}$
 $A = \frac{O}{\tan\theta}$

$v_f = v_i + at$

Solve for v_i

$v_f = v_i + at$
 $-at -at$
 $v_f - at = v_i$
 $v_i = v_f - at$

Subtract "at" from both sides
Mirror

$v = v_0 \pm at$

0 = at time zero
 \pm : +ve "a", -ve "a"

$v_f = v_i + at$
 $v_i = v_f - at$

Bring it over
 Change sign
 Mirror

Solve for "t"

$v_f = v_i + at$
 $v_f - v_i = at$
 $\frac{v_f - v_i}{a} = \frac{at}{a}$
 $t = \frac{v_f - v_i}{a}$

Subtract v_i from both sides
 Divide both sides by "a"
 Mirror

$v_f = v_i + at$
 $t = \frac{v_f - v_i}{a}$

Bring "v₀" over
 Bring "a" down
 Mirror

P11 - 1.3 - Isolating variables *Notes* Algebra

$$\boxed{a^2 + b^2 = c^2} \quad \text{Solve for } c$$

$$a^2 + b^2 = c^2$$

$$\sqrt{a^2 + b^2} = \sqrt{c^2} \quad \text{Square root both sides}$$

$$\sqrt{a^2 + b^2} = c \quad \text{Mirror}$$

$$\boxed{c = \sqrt{a^2 + b^2}}$$

Solve for "a"

$$a^2 + b^2 = c^2$$

$$a^2 = c^2 - b^2 \quad \text{Bring } b^2 \text{ over}$$

$$\sqrt{a^2} = \sqrt{c^2 - b^2} \quad \text{Square root both sides}$$

$$\boxed{a = \sqrt{c^2 - b^2}}$$

$$\boxed{v_f^2 = v_i^2 + 2ad}$$

Solve for v_f

$$v_f^2 = v_i^2 + 2ad$$

$$\sqrt{v_f^2} = \sqrt{v_i^2 + 2ad}$$

$$\boxed{v_f = \sqrt{v_i^2 + 2ad}}$$

Square root both sides

Solve for v_i

$$v_f^2 = v_i^2 + 2ad$$

$$v_f^2 - 2ad = v_i^2$$

$$\sqrt{v_f^2 - 2ad} = v_i$$

$$\boxed{v_i = \sqrt{v_f^2 - 2ad}}$$

Bring 2ad over
Square root both sides

Solve for "a"

$$v_f^2 = v_i^2 + 2ad$$

$$v_f^2 - v_i^2 = 2ad$$

$$\frac{v_f^2 - v_i^2}{2d} = a$$

$$\boxed{a = \frac{v_f^2 - v_i^2}{2d}}$$

Bring v_i^2 over
Bring 2a down

Solve for d

$$v_f^2 = v_i^2 + 2ad$$

$$v_f^2 - v_i^2 = 2ad$$

$$\frac{v_f^2 - v_i^2}{2a} = d$$

$$\boxed{d = \frac{v_f^2 - v_i^2}{2a}}$$

Bring v_i^2 over
Bring 2d down

$$\boxed{d = v_i t + \frac{1}{2} a t^2}$$

Solve for a

$$d = v_i t + \frac{1}{2} a t^2$$

$$d - v_i t = \frac{1}{2} a t^2 \quad \text{Bring } v_i t \text{ over}$$

$$\frac{2(d - v_i t)}{t^2} = a \quad \text{Bring 2 up (Brackets!)}$$

$$\boxed{a = \frac{2(d - v_i t)}{t^2}} \quad \text{Bring } t^2 \text{ down}$$

Solve for t

$$d = v_i t + \frac{1}{2} a t^2$$

$$0 = \frac{1}{2} a t^2 + v_i t - d$$

$$\boxed{\text{Quadform}}$$

Solve for v_i

$$d = v_i t + \frac{1}{2} a t^2$$

$$d - \frac{1}{2} a t^2 = v_i t \quad \text{Bring } \frac{1}{2} a t^2 \text{ over}$$

$$\frac{d - \frac{1}{2} a t^2}{t} = v_i \quad \text{Bring } t$$

$$\boxed{v_i = \frac{d - \frac{1}{2} a t^2}{t}}$$