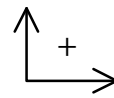


P11 - 3.1 - $F = ma$ Newton's Laws Notes



Force - A Push or pull

Force of Gravity - Attracts Matter to Matter

Four Fundamental Forces

Matter - Anything that has Mass and takes up space.

1. Gravitational P11

Mass - Amount of Matter an object holds

2. Electromagnetic (e^-)

Weight - The force of Gravitational Attraction

3. Strong Nuclear (keeps p^+ in nucleus)

Mass is **constant** throughout the universe.

4. Weak Nuclear (Radioactive Decay)

Weight **depends** on your location. (Earth, Moon, Space ...)
 g , depends on the m of the planet and d from it's centre

Units: Newton's (N)

1 Newton: The force required to accelerate a 1kg object at $1 \frac{m}{s^2}$.

$$1N = \frac{1kgm}{s^2} \quad F = ma \quad N = kg \frac{m}{s^2}$$

Newton's 3 Laws:

Including at rest

1 Inertia - An object will continue at a constant velocity, unless acted upon by a non-zero sum force.

$$F_{net} = ma$$

2 The sum of the forces in the direction of motion, minus opposing forces.

$$\Sigma F = ma$$

$$F_a - F_f = ma$$

(Winners minus losers.)

Tug of War

3 Every force has an equal and opposite force. (You push me, I push back)

The Gravitational Force:

$$F_g = mg$$

F_g : Force of Gravity, (Gravitational Force)

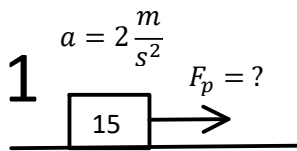
m : Mass

g : Gravity

$$g = -9.8 \frac{m}{s^2}$$

$$\frac{N}{kg} = \frac{m}{s^2}$$

What is the Pull Force required to accelerated a 15kg object at $2 \frac{m}{s^2}$?



F_n : Normal Force (Weight)

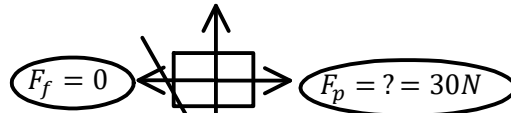
F_p : Force Pull

F_f : Force of Friction

2 FBD Free Body Diagram:

$$F_n = F_g^*$$

$$F_n = 147N \quad F_n = F_g^*, \theta = 0$$



3

$$F = ma$$

$$F = (15)(2)$$

$$F = 30N$$

$$F_{net} = ma$$

$$F_p - F_f = ma$$

$$F_p - 0 = 15 \times 2$$

$$F_p = 30N$$

We were actually supposed to subtract a non-existent Frictional Force.

1st

$$F_g = mg$$

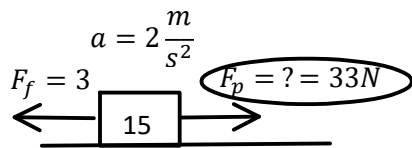
$$F_g = 15 \times 9.8$$

$$F_g = 147N$$

$$g = 9.8 \frac{m}{s^2}$$

+ve downward!

What is the Pull Force required to Accelerated a 15kg object at $2 \frac{m}{s^2}$, with a F_f of 3 N?



$$F = ma$$

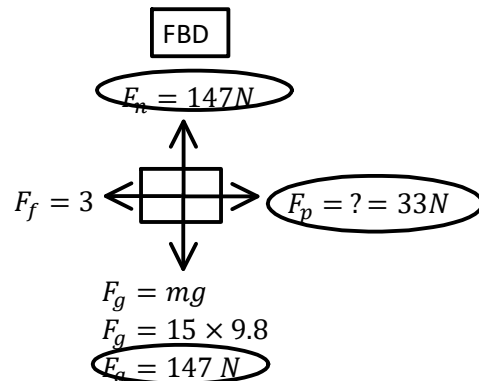
$$F_p - F_f = ma$$

$$F_p - 3 = ma + F_f$$

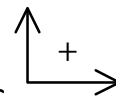
$$F_p = 30 + 3$$

$$F_p = 33N$$

Obviously 3 more Newton's than without Friction = 3N.



P11 - 3.2 - $F = ma$, $F_f = \mu F_n$ Solve Variable Notes



A Pull Force of 45 N is applied to a 15kg object. Find its acceleration.

$a = ? = 3$

$F_p = 45$

15

FBD

$F_n = 147N$

$F_f = 0$

$F_p = 45N$

$F_g = mg$
 $F_g = 15 \times 9.8$
 $F_g = 147N$

$F = ma$
 $a = \frac{F}{m}$
 $a = \frac{45}{15}$
 $a = 3 \frac{m}{s^2}$

A Push Force of 12 N on an object's $a = 2 \frac{m}{s^2}$, Find object's Mass and Weight?

$a = 2 \frac{m}{s^2}$

$F_p = 12$

6

FBD

$F_n = 58.8N$

$F_f = 0$

$F_p = 12N$

$F_g = mg$
 $F_g = 6 \times 9.8$
 $F_g = 58.8N$

$F = ma$
 $m = \frac{F}{a}$
 $m = 6kg$

Cross it out

Weight = F_n

A Pull Force of 92 N on a 15 kg object's $a = 5 \frac{m}{s^2}$. What is the Frictional Force?

$a = 5 \frac{m}{s^2}$

$F_f = ?$

15

$F_p = 92$

FBD

$F_n = 147N$

$F_f = ? = 92$

$F_p = 92N$

$F_g = mg$
 $F_g = 15 \times 9.8$
 $F_g = 147N$

$F = ma$
 $F_p - F_f = ma$
 $F_f = F_p - ma$
 $F_f = 92 - 15 \times 5$
 $F_f = 17N$

How far did the object go in 5s?

$$\Delta d = v_i t + \frac{1}{2} a t^2$$

$$d = (0)t + \frac{1}{2} (5)(5)^2$$

$$d = 62.5 m$$

Acceleration is the Kinematics - Dynamics Link

t	d
0	0
1	2.5
2	10
3	22.5
4	40
5	62.5

What is the velocity after 2 seconds?

$$v_f = v_i + at$$

$$v_f = 0 + 5(2)$$

$$v_f = 10 \frac{m}{s}$$

How long until it reaches $25 \frac{m}{s}$.

$$v_f = v_i + at$$

$$25 = 0 + 5t$$

$$t = 5s$$

t	v
0	0
1	5
2	10
3	15
4	20
5	25

Find the Push Force to $a = 2 \frac{m}{s^2}$ a 15kg object, with a Frictional Co-efficient of $\mu = 0.3$?

$a = 2 \frac{m}{s^2}$

$F_f = ? = 44.1$

15

$F_p = 92$

$\mu = 0.3$

FBD

$F_n = 147N$

$F_f = ? = 44.1$

$F_p = 74.1N$

$F_g = mg$
 $F_g = 15 \times 9.8$
 $F_g = 147N$

$F_f = \mu F_n$
 $F_f = 0.3 \times 147$
 $F_f = 44.1N$

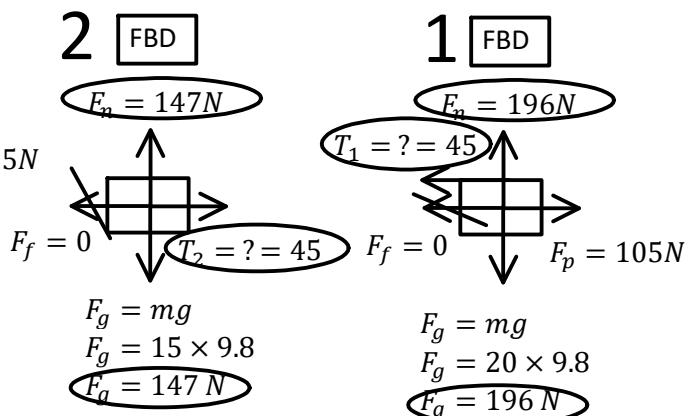
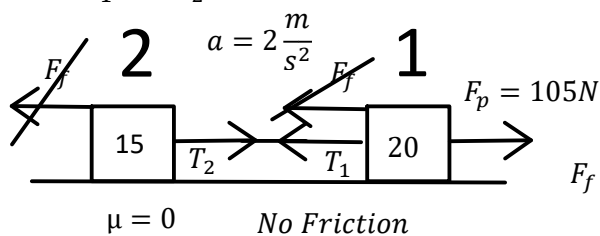
$F = ma$
 $F_p - F_f = ma$
 $F_p = ma + f_f$
 $F_p = 15 \times 2 + 44.1$
 $F_p = 74.1N$

μ : Frictional Co-efficient (Mhew) No Units.

Higher the Mhew, μ , Higher the Frictional Force.

P11 - 3.3 - Tension Notes

Find T_1 and T_2



System Mass of system

$$F = ma$$

$$F - T_1 - F_f + T_2 - F_f = ma$$

$$105 - \cancel{T_1} - \cancel{F_f} + \cancel{T_2} - \cancel{F_f} = (15 + 20)a$$

$$105 = 35a$$

$$a = 3 \frac{m}{s^2}$$

$T_1 = T_2$

Mass 2

$$F = ma$$

$$T_2 - \cancel{F_f} = ma$$

$$T_2 - 0 = 15 \times 3$$

$$T_2 = 45 \text{ N}$$

Mass 1

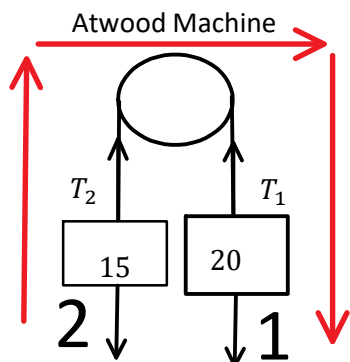
$$F = ma$$

$$F - \cancel{T_1} - \cancel{F_f} = ma$$

$$105 - T_1 - F_f = 20 \times 3$$

$$T_1 = 45 \text{ N}$$

Tension must be equal!



$$F_g = mg$$

$$F_g = 15(9.8)$$

$$F_g = 147 \text{ N}$$

$$F_g = mg$$

$$F_g = 20(9.8)$$

$$F_g = 196 \text{ N}$$

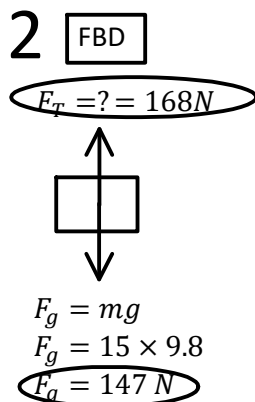
$$F = ma$$

$$Fg_1 - T_1 + T_2 - Fg_2 = ma$$

$$196 - \cancel{T_1} + \cancel{T_2} - 147 = (15 + 20)a$$

$$49 = 35a$$

$$a = 1.4 \frac{m}{s^2}$$



Mass 2

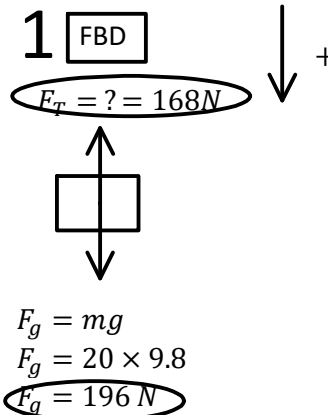
$$F = ma$$

$$T_2 - F_g = ma$$

$$T_2 = ma + F_g$$

$$T_2 = 15 \times 1.4 + 147$$

$$T_2 = 168 \text{ N}$$



Mass 1

$$F = ma$$

$$F_g - T_1 = ma$$

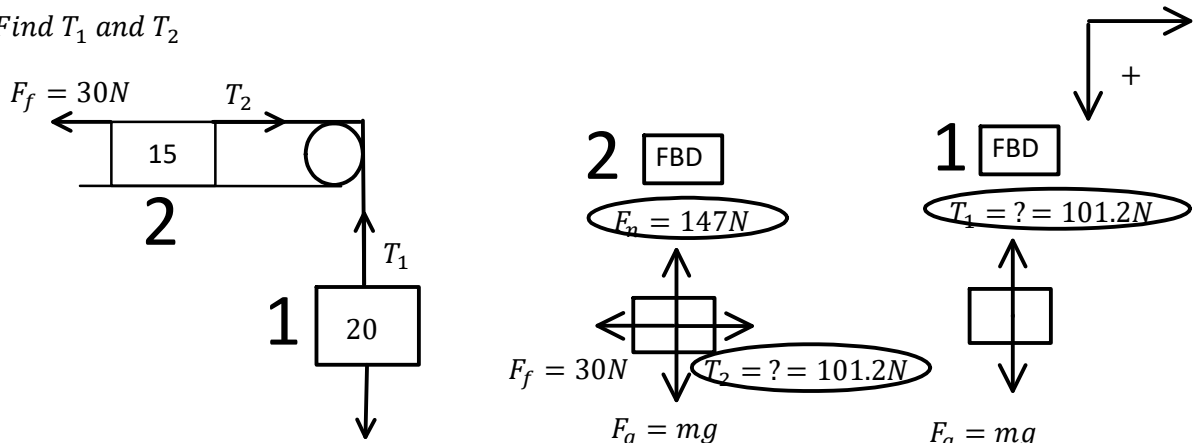
$$T_1 = F_g - ma$$

$$T_1 = 196 - 20 \times 1.4$$

$$T_1 = 168 \text{ N}$$

P11 - 3.3 - Tension Notes

Find T_1 and T_2



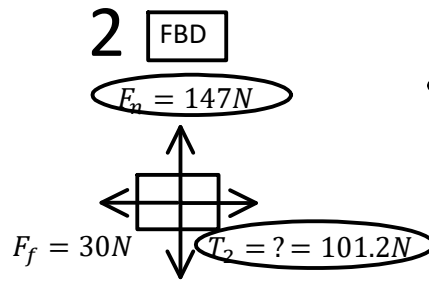
$$F = ma$$

$$F_g - T_1 + T_2 - F_f = ma$$

$$196 - 30 = (20 + 15)a$$

$$166 = 35a$$

$$a = 4.74 \frac{m}{s^2}$$



$$F_g = mg$$

$$F_g = 15 \times 9.8$$

$$F_g = 147 \text{ N}$$

Mass 2

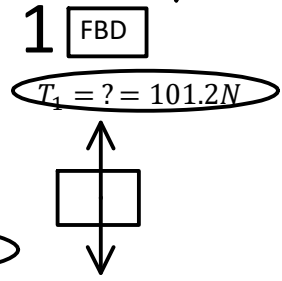
$$F = ma$$

$$T_2 - F_f = ma$$

$$T_2 = ma + F_f$$

$$T_2 = 15 \times 4.74 + 30$$

$$T_2 = 101.2 \text{ N}$$



$$F_g = mg$$

$$F_g = 20 \times 9.8$$

$$F_g = 196 \text{ N}$$

Mass 1

$$F = ma$$

$$F_g - T_1 = ma$$

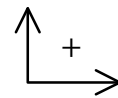
$$T_1 = F_g - ma$$

$$T_1 = 196 - 20 \times 4.74$$

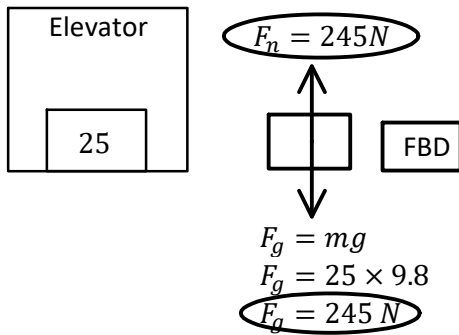
$$T_1 = 101.2 \text{ N}$$

P11 - 3.4 - Elevator Notes

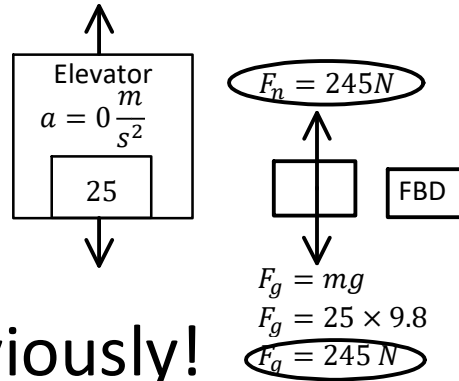
Logic



Find the weight of a 25 kg object on a scale in a stationary Elevator?

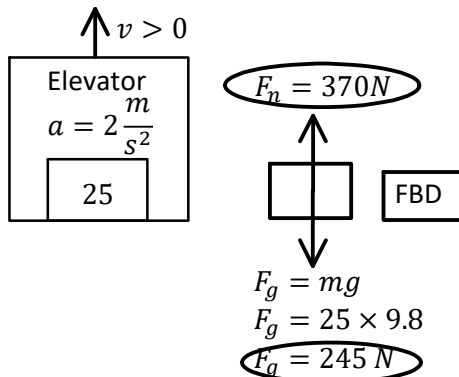


What is the weight of a 25 kg object on a scale in a Elevator moving at a constant velocity?



Obviously!

Find the weight of a 25 kg object on a scale in an Elevator moving up, $a = 5 \frac{m}{s^2}$ upwards.



$$F_{net} = ma$$

$$F_n - F_g = ma$$

$$F_n = ma + F_g$$

$$F_n - 245 = (25)(5) + 245$$

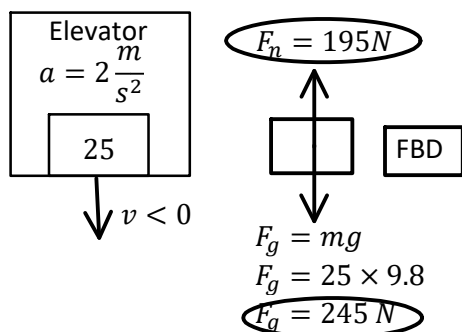
$$F_n = 370 N$$

Obviously you would be Heavier

Or going up slowing down

Obviously!

Find the weight of a 25 kg object on a scale in an Elevator moving down, $a = 2 \frac{m}{s^2}$ downward.



$$F_{net} = ma$$

$$F_g - F_n = ma$$

$$F_n = F_g - ma$$

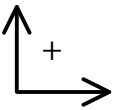
$$F_n = 245 - (25)(2)$$

$$F_n = 195 N$$

Obviously you would be Lighter

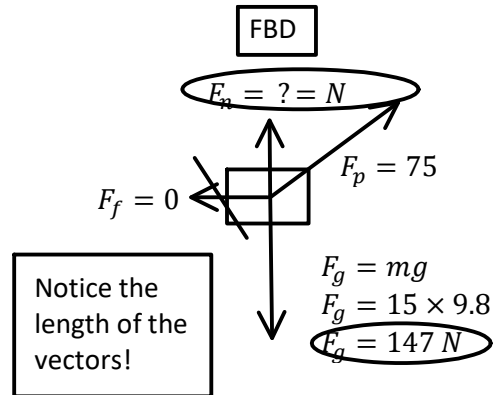
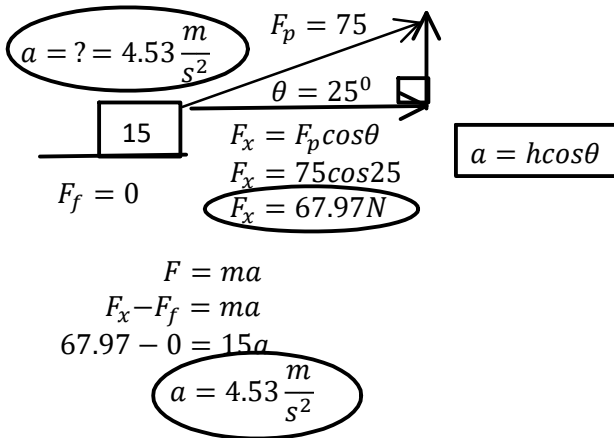
Or going down speeding up

Obviously!

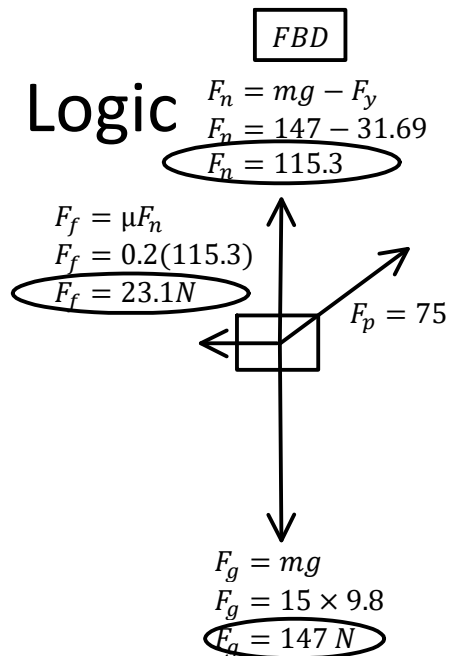
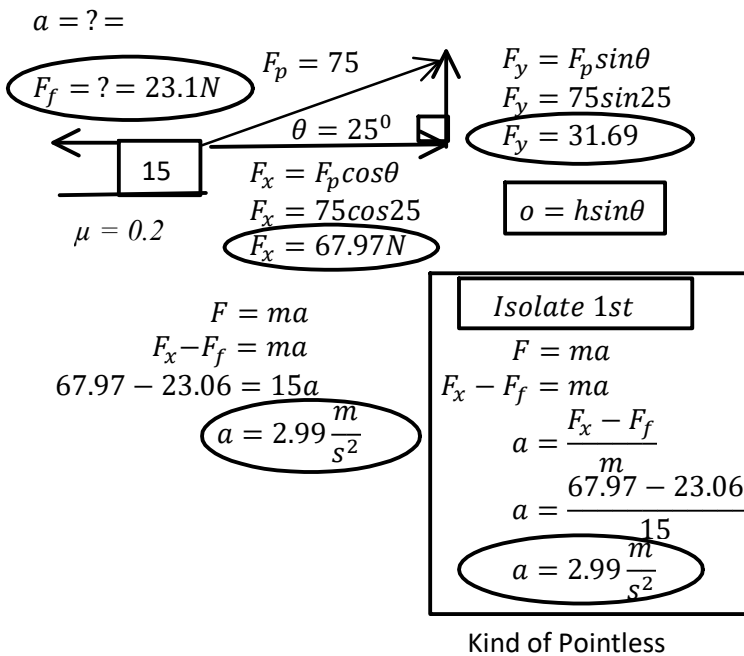


P12 - 3.5 - Dynamics Trig Notes

Find the acceleration of a $F = 75\text{ N}$ on a 15 kg object pulled at an angle of 25° in diagram?



Find the "a" of a $F = 75\text{ N}$ on a 15 kg object pulled at an angle of 25° and $\mu = 0.2$ in diagram.



What takes less force to pull or push a lawn mower? Pull, because pushing loses force to the ground!

P12 - 3.6 - Dynamics Fric Slope Notes

What is the acceleration of a 15 kg block sliding down a 30° slope? Ignore Friction.

$F_f = \mu F_n; \mu = 0$
 $F_f = 0$
 (F_n useless)

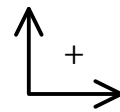
F_g : Straight Down
 : Perpendicular (90°) to Surface
 : Parallel to Surface

$F_g = mg$	$F_x = F_g \sin\theta$	$F = ma$
$F_g = 15(9.8)$	$F_x = mg \sin 30$	$F_x - F_f = ma$
$F_g = 147$	$F_x = 147(.5)$	$73.5 - 0 = 15a$
	$F_x = 73.5$	$a = 4.9 \frac{m}{s^2}$

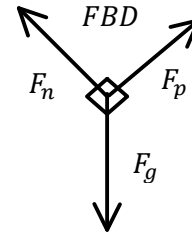
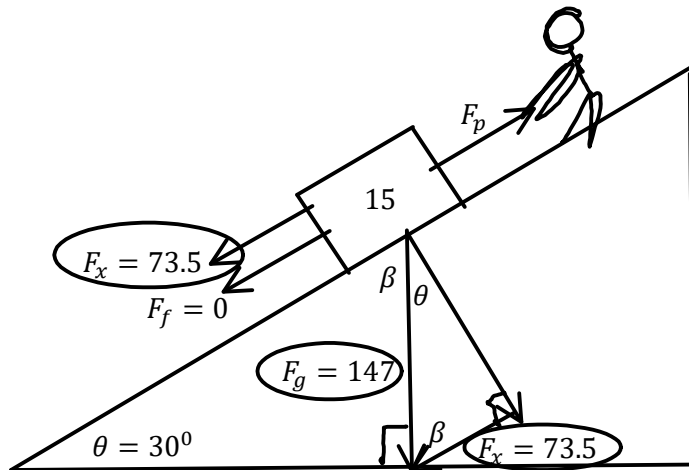
What is the acceleration of a 15 kg block sliding down a 30° slope with $\mu = 0.3$.

$F_g = mg$	$F_x = F_g \sin\theta$	$F = ma$
$F_g = 15(9.8)$	$F_x = mg \sin 30$	$F_x - F_f = ma$
$F_g = 147$	$F_x = 147(.5)$	$73.5 - 38.19 = 15a$
	$F_x = 73.5$	$a = 2.35 \frac{m}{s^2}$

P12 - 3.6 - Dynamics Pull Fric Slope Notes



How much force is required to accelerate a 15 kg object at $2 \frac{m}{s^2}$ up a slope 30° with $\mu = 0$?



$$F_g = mg$$

$$F_g = 15(9.8)$$

$$F_g = 147$$

$$F_x = F_g \sin \theta$$

$$F_x = 147 \sin 30$$

$$F_x = 73.5$$

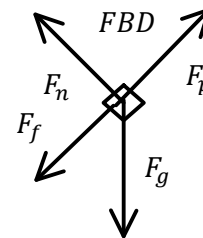
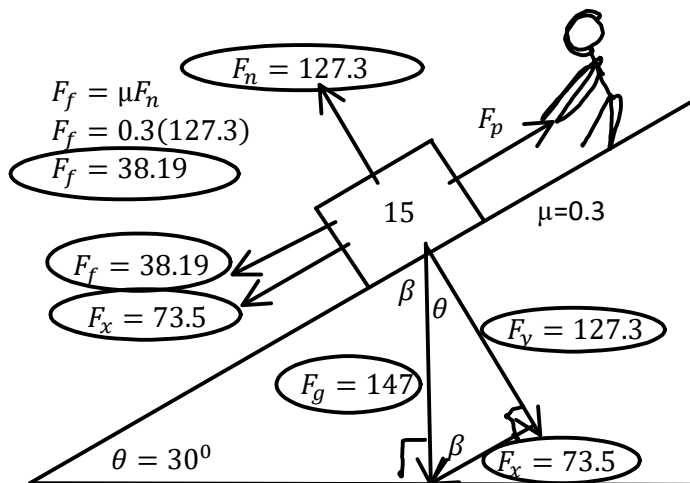
$$F = ma$$

$$F_p - F_x - F_f = ma$$

$$F_p - 73.5 = 15(2)$$

$$F_p = 103.5 \text{ N}$$

How much force is required to accelerate a 15 kg object at $2 \frac{m}{s^2}$ up a slope 30° with $\mu = 0.3$?



$$F_f = \mu F_n$$

$$F_f = 0.3(127.3)$$

$$F_f = 38.19$$

$$F_f = 38.19$$

$$F_x = 73.5$$

$$F_g = 147$$

$$F_y = 127.3$$

$$F_y = F_g \cos \theta$$

$$F_y = mg \cos \theta$$

$$F_y = 147(.866)$$

$$F_y = 127.3 \text{ N}$$

$$F_g = mg$$

$$F_g = 15(9.8)$$

$$F_g = 147$$

$$F_x = F_g \sin \theta$$

$$F_x = 147 \sin 30$$

$$F_x = 73.5$$

$$F = ma$$

$$F_p - F_x - F_f = ma$$

$$F_p - 73.5 - 38.19 = 15(2)$$

$$F_p = 141.69 \text{ N}$$

P12 - 3.6 - Dynamics Pulley Fric Up Slope Notes

Find the acceleration of the system and the tension T_1 and T_2 .

$F_f = \mu F_n$
 $F_f = 0.3(127.3)$
 $F_f = 38.19$

$F_n = 127.3$
 $F_x = 73.5$
 $F_f = 38.19$
 $F_g = 147$
 $F_y = 127.3$
 $F_x = 73.5$
 $\theta = 30^\circ$
 $\mu = 0.3$

$F_{g1} = mg$
 $F_{g1} = 25(9.8)$
 $F_{g1} = 245$

$F_{g2} = mg$
 $F_{g2} = 15(9.8)$
 $F_{g2} = 147$

$F_x = F_g \sin \theta$
 $F_x = mg \sin 30$
 $F_x = 147(.5)$
 $F_x = 73.5$

$F_y = F_g \cos \theta$
 $F_y = mg \cos \theta$
 $F_y = 147(.866)$
 $F_y = 127.3 \text{ N}$

$F_{g1} > F_{g2}$

Mass 2
 $F = ma$
 $T_2 - F_x - F_f = ma$
 $T_2 - 73.5 - 38.19 = 15 \times 3.3$
 $T_2 = 161.19 \text{ N}$

Mass 1
 $F = ma$
 $Fg - T_1 = ma$
 $245 - T_1 = 25 \times 3.3$
 $T_1 = 162.5 \text{ N}$

$F_{g1} - T_1 + T_2 - F_x - F_f = ma$
 $245 - 73.5 - 38.19 = 40a$
 $a = 3.3 \frac{m}{s^2}$

$F_n = 1273.06$
 $F_f = 381.92$
 $F_x = 735$
 $F_g = 1470$
 $F_y = 1273.06$
 $F_x = 735$
 $\theta = 30^\circ$
 $\mu = 0.3$

$F_{g2} = mg$
 $F_{g2} = 25(9.8)$
 $F_{g2} = 245$

$F_{g1} = mg$
 $F_{g1} = 150(9.8)$
 $F_{g1} = 1470$

$F_x = F_g \sin \theta$
 $F_x = mg \sin 30$
 $F_x = 1470(.5)$
 $F_x = 735$

$F_y = F_g \cos \theta$
 $F_y = mg \cos \theta$
 $F_y = 1470(.866)$
 $F_y = 1273.06 \text{ N}$

$F_f = \mu F_n$
 $F_f = 0.3(1273.06)$
 $F_f = 381.92$

$F_{g1} \gg F_{g2}$

Mass 1
 $F = ma$
 $F_x - F_f - T_2 = ma$
 $735 - 381.92 - T_2 = 15(2.7)$
 $T_2 = 313.5 \text{ N}$

Mass 2
 $F = ma$
 $T_2 - F_g = ma$
 $T_2 - 245 = 25(2.7)$
 $T_1 = 312.5 \text{ N}$

$F_x - F_f - T_2 + T_1 - F_{g2} = ma$
 $735 - 381.92 - 245 = 40a$
 $a = 2.7 \text{ N}$