

S12 - 0.0 - Probability Cheat Sheet

Logic Guess and Check

Venn Diagrams

$$A \cup B = A + B - A \cap B$$

$$A \cup B = A + B \quad \text{Mutually Exclusive} \quad A \cap B = 0$$

$$A \cup B \cup C = A + B + C - A \cap B - A \cap C - B \cap C + A \cap B \cap C$$



Set Notation

And : \cap Not : $\bar{\cap}$ $\bar{A} = A'$
Or : \cup

Demorgan's Law

$$\bar{A} \cap \bar{B} = \overline{A \cup B} \quad \overline{(\bar{A} \cap \bar{B})} = A \cup B$$

$$\bar{A} \cup \bar{B} = \overline{A \cap B} \quad \overline{(\bar{A} \cup \bar{B})} = A \cap B$$

Probability $P(A) =$ Probability of Event A

$$P(A) = \frac{\# \text{ Favourable Events}}{\text{Sample Space}}$$

$$P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

Bays Theorem

$$P(A|B) = \frac{P(A \cap B)}{P(B)}$$

$(A|B)$; A Given B

Independence $P(B|A) = P(B)$ given: |

$$P(A|B) = \frac{P(B|A) \times P(A)}{P(B|A) \times P(A) + P(B|\bar{A}) \times P(\bar{A})}$$

$$P(A \cup B) = 1 - P(\bar{A} \cap \bar{B}) \quad P(\bar{A}) = 1 - P(A) \quad \text{Compliment}$$

$$P(B|A) \neq P(A|B)$$

$$P(A \cup B) = P(A) + P(B) \quad \text{Mutually Exclusive} \quad P(A \cap B) = 0$$

$$P(A \cap B) = P(A)P(B) \quad \text{Independent} \quad P(B|A) = P(B)$$

$P(A, B)$: Probability of A then B

Probability of an Event must be between 0 and 1. $0 \leq P(A) \leq 1$

$$P_1 + P_2 + \dots + P_n = 1 \quad \sum P(x) = 1$$

$P(\text{certain}) = 100\%$
 $P(\text{impossible}) = 0\%$

$$P(x \geq 1) = 1 - P(\text{none})$$

$$P(x \geq 2) = 1 - P(x \leq 1)$$

$$P(x \geq A) = 1 - P(x \leq (A - 1))$$

5% Rule (w/w/out rep)
Sample $\leq 5\%$ of population
Dependent \rightarrow Independent

Fundamental Counting Principle

$$a \times b \times c$$

Factorial Notation!

Repeats?

Blanks $_ _ _ , _ _ _ , _ _ _$

$\frac{\# \text{ options}}{\text{options}}$

$$\times \div 2 \text{ or } \#!$$

with/replacement/w/out rep
Given!

Tree Diagrams

Table

$(\text{outcomes per trial})^{\text{number of trials}}$

All - None

Multiply Branches

Add Leaves

Cannot = All - Can

Cases! Cases: Multiply within cases, add separate cases.

Circle: $(n - 1)!$

Identical Objects

$$\frac{(\# \text{ of letters})!}{(\text{repeating letter})! (\text{other repeating letter})! \dots}$$

$$\text{Paths in Squares: } \frac{(l + w)!}{l! w!}$$

$$\text{Paths in Cubes: } \frac{(l + w + h)!}{l! w! h!}$$

Combinatorics Formulas

$$n \geq r$$

Permutations: Order Matters

Combinations: Doesn't Matter

$${}_n P_r = \frac{n!}{(n - r)!}$$

$${}_n C_r = \frac{n!}{r!}$$

$${}_n C_r = \frac{n!}{r! (n - r)!}$$

$$\binom{n}{r}$$

Binomial Theorem

$$t_{k+1} = {}_n C_k a^{n-k} b^k$$

$$; (a + b)^n$$

; $n + 1$ terms

; k is always one less than the term number.

Odds

Favourable Outcomes : Unfavourable Outcomes $\frac{\text{part} : \text{part}}$