# C12-5.4 - Int Def/Area/Bet/Vol/xyAxis 

Find the Area between the curve $y=x^{2}$ and the $x$ - axis $0 \leq x \leq 1$.

Find the Area between the curve
$y=\sqrt{x}$ and the $x$ - axis $0 \leq x \leq 4$.

Find the Area between the curve $y=x^{2}-x$ and the x - axis $0 \leq x \leq 2$.

Find the Area between the curve $y=$ $\cos \left(\frac{1}{2} x\right)$ and the $x$ - axis $0 \leq x \leq \pi$.

Find the Area between the curve $y=$ $\left|\mathrm{x}^{2}-4\right|$ and the x - axis $-3 \leq x \leq 3$.

Find the Area below the curve $x^{2}+$ $y^{2}=4$ and above the $x$ - axis.

Find the area between the curves
$y=x \& y=x^{2}$

Find the Volume of revolution
$y=x$
$0 \leq x \leq 4$

Find the Volume of revolution between the two functions $y=$ $\sqrt{x} \& y=\frac{1}{2} x, 0 \leq x \leq 4$, around the x -axis.

Find the area between the curves

$$
y=x^{2} \& y=4
$$

Find the Volume of revolution between the two functions $y=x+2 \& y=2,0 \leq x \leq$ 4 , around the axis $y=1$.

Find the Volume of revolution between the two functions $y=x^{2} \& y=2 x$ around the $y$-axis.

## C12-5.4-Int Info/Graph/Ave Rev

$$
\begin{array}{ll}
\int_{0}^{2} f(x) d x=2 & \int_{2}^{3} f(y) d y=-1 \\
\int_{2}^{0} f(x) d x=? & \int_{1}^{3} \frac{1}{2} f^{2}(x) d x=? \\
\int_{0}^{3} f(x) d x=? & \int_{0}^{3}(f(x)+2 g(x)) d x=?
\end{array}
$$



A function $f(x)$ consists of straight lines and quarter circles.

$$
\begin{array}{ll}
\int_{-4}^{0} f(x) d x=? & \int_{0}^{2} f(x) d x=? \\
\int_{2}^{4} f(x-1) d x=? & \int_{2}^{4} f(2 x) d x=?
\end{array}
$$

Find the average value over the interval and where it occurs.
$y=4-x^{2}, 0 \leq x \leq 2$
$y=\sqrt{9-x^{2}},-3 \leq x<3$

